

QUANTUM NUMBER

DENSITY

ASYMMETRIES

IN

Q

C

D

JETS

CORRELATED

WITH



SPIN

d. sivers u. mich &
Port. Phys. Ins.

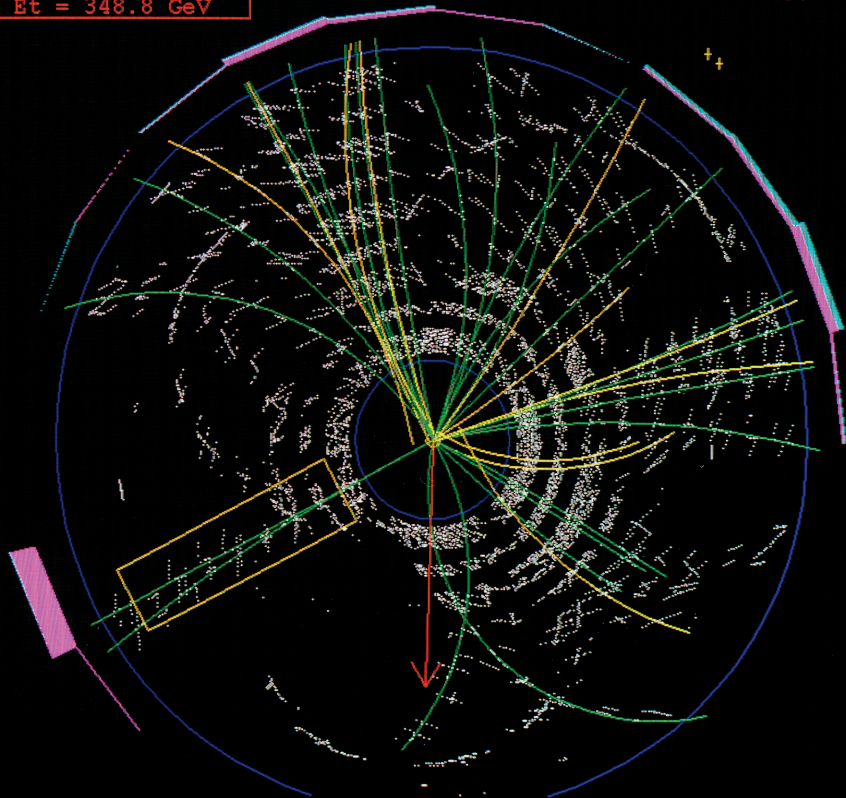
$\cancel{E}_t(\text{METS}) = 56.2 \text{ GeV}$
 $\Phi = 268.5 \text{ Deg}$
 $\text{Sum } E_t = 348.8 \text{ GeV}$

$+++$

$E_{\text{max}} = 125.7 \text{ GeV}$

$++$

$+$



OUTLINE

- I, PQCD & Jets in final state of hard-scattering processes - Are QCD jets "hawser-laid?"
- II, Transverse spin - a probe of confinement & chiral-symmetry breaking
- III, $\Delta_{0\uparrow} \Rightarrow p\pi^-$ and the orientation of the jet fragmentation process
- IV, Spin-directed momentum & density asymmetries a tool for studying MEDIUM MODIFICATION of QCD dynamics [arXiv:1106.3947](https://arxiv.org/abs/1106.3947) (PRD)
- V, Detector requirements & other spin-directed measurements

(HAWSER ROPE)

A hawser is a 3-stranded twisted rope. In nautical english, the process of manufacturing rope from a length of fibres is called "laying"



Z

hawser have
2 chiral
enantiomers
(as in S,R
enantiomers of
molecular physics)



S

Unlike fundamental "strings" ropes have internal structure. The internal structure of QCD jets provides information about confinement & chiral symmetry breaking.

I. PQCD & JETS



The study of QCD jets is a mature "ish" discipline

Jet Algorithms { K_T , $\cancel{K_T}$
SIScone, ... }

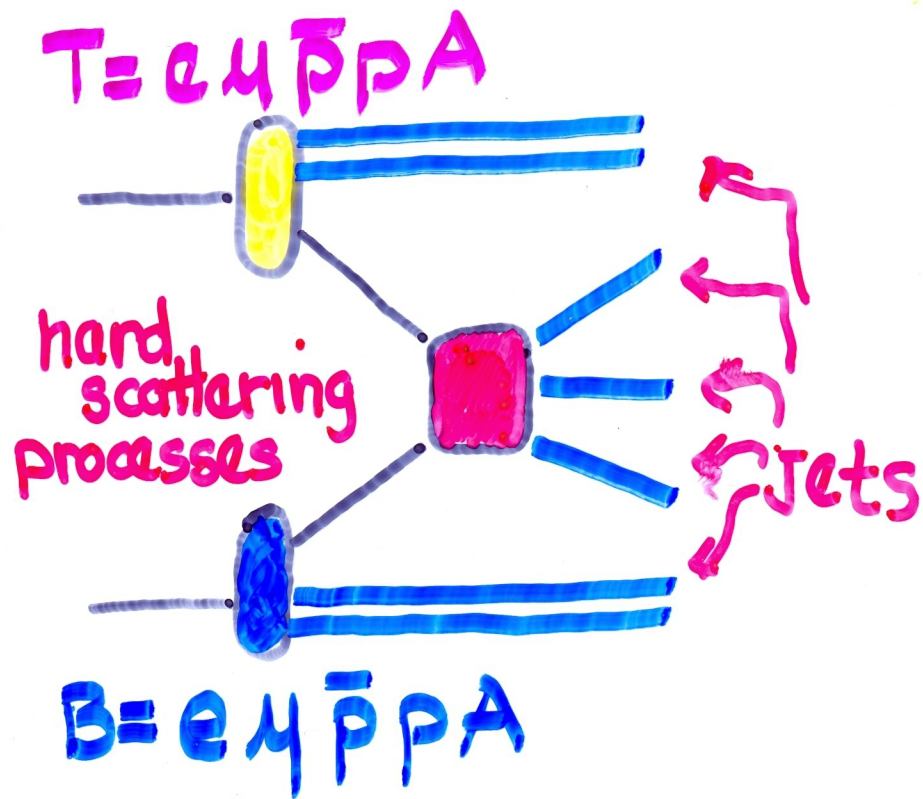
— Monte Carlo

{ Herwig ---
Pythia --- }

are packaged for each detector

FASTJET, ...

to include detector acceptances, correct for neutral particles, etc.



$$e^+e^- \rightarrow \text{jets}$$

$$ep \rightarrow e' + \text{jets}$$

$$\bar{p}p \rightarrow \text{jets}$$

$$pp \rightarrow \text{jets}$$

$A = \text{heavy nucleus}$

$$eA \rightarrow e' + \text{jets}$$

$$\bar{p}A \rightarrow \text{jets}$$

$$pA \rightarrow \text{jets}$$

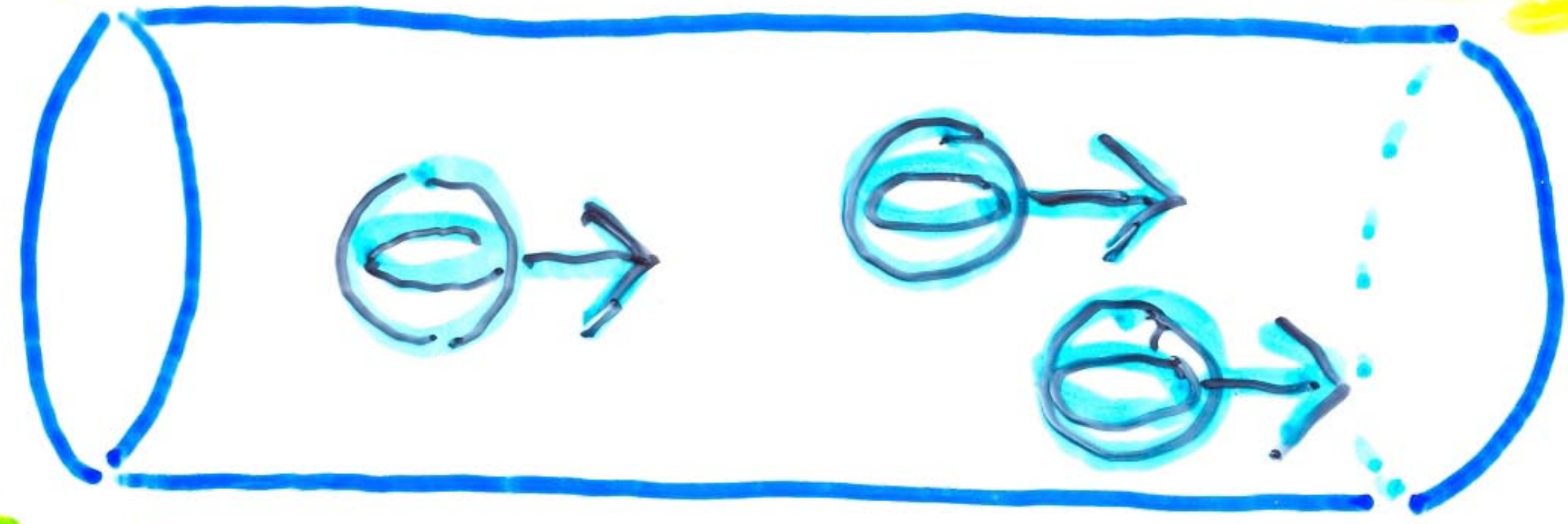
$$AA \rightarrow \text{jets}$$

QCD jets are highly virtual hadronic systems

that cannot be studied via ab initio calculations involving lattice simulations

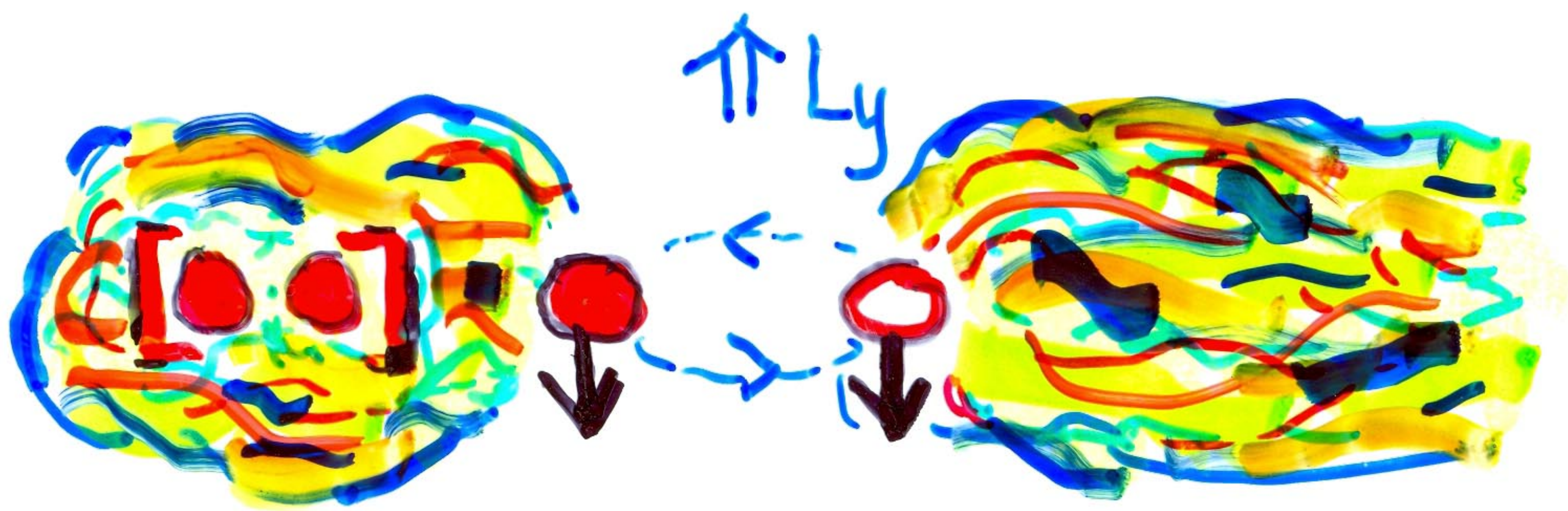
The study of jets supplements the study of hadronic spectroscopy.

NonAbelian Field Strength



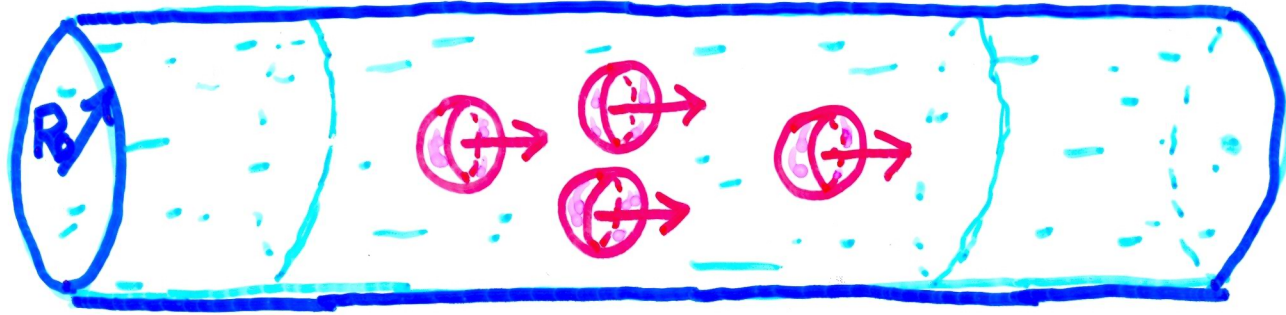
$$U_1 \in SU_2 \in SU_3$$

Description of an Expanding
Cylindrical Flux



Configuration

Classical non-Abelian Fields with Cylindrical Symmetry



$$(t, \hat{r}, \hat{\phi}, \hat{z})$$

$$(\hat{r}, \hat{\phi}, \hat{z})$$

$$U_1 \in SU_2 \in SU_3$$

$$\hat{r} = (1, 0, 0)$$

$$\hat{\phi} = (0, 1, 0)$$

$$\hat{z} = (0, 0, 1)$$

$$\xi_{ia} = \hat{z}_i \hat{z}_a = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\delta_{ia}^T = (1 - \xi_{ia}) = \hat{r}_i \hat{r}_a + \hat{\phi}_i \hat{\phi}_a = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\varepsilon_{ia}^T = \varepsilon_{ial} \hat{z}_l = \hat{r}_i \hat{\phi}_a - \hat{\phi}_i \hat{r}_a = \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

gauge transformation $\Omega(\vec{r}, \vec{z}, t) = \exp \left\{ i g \frac{\gamma_a}{2} \hat{z}_a \theta_a(\vec{r}, \vec{z}, t) \right\}$

spatial rotations $R(\vec{r}, \vec{z}, t) = \exp \left\{ i \frac{\sigma_i}{2} \hat{z}_i \theta_i(\vec{r}, \vec{z}, t) \right\}$

{ START WITH ANSATZ }

(Ralston
Sivers)

$$gA_0^a = A_0(r, z, t) \hat{z}_a$$

$$gA_i^a = A_1(r, z, t) \xi_{ia} + a(r, z, t) \sin[\omega(r, z, t)] \delta_{ia}^T + \{a(r, z, t) \cos[\omega(r, z, t)] - 1\} \varepsilon_{ia}^T$$

stay away from ends of cylinder & look for solutions to non-Abelian Maxwell's eqns. that display

confinement in radial direction $r > R_0$
simple boundary conditions

$$\left\{ \begin{array}{l} A_0 = A_1 = 0 \\ a = -1 \quad \cos \omega = -1 \end{array} \right\} \quad r > R_0 + 2\Delta \quad \text{all } z, t$$

Further Simplify by Abelianizing Core of Cylinder

$$\left\{ \begin{array}{l} A_0(r, z, t) = A_0(z, t) \\ A_1(r, z, t) = A_1(z, t) \end{array} \right. \quad \left\{ \begin{array}{l} a(r, z, t) = a_0 = \text{const} \\ \omega(r, z, t) = \omega(z, t) \end{array} \right. \quad r < R_0$$

$$\partial_i^{ab} \hat{z}_b = (\partial_i \delta^{ab} + \epsilon^{abc} A_i^c) \hat{z}_b = a_0 e_{ia}^S [\omega(z, t)]$$

$$= a_0 \{ \delta_{ia}^T \cos \omega(z, t) - \epsilon_{ia}^T \sin \omega(z, t) \}$$

$$-i [\hat{z}, \partial_i \hat{z}]^a = a_0 e_{ia}^A [\omega(z, t)] = a_0 \{ \delta_{ia}^T \sin \omega(z, t) + \epsilon_{ia}^T \cos \omega(z, t) \}$$

$e_{ia}^S(\omega)$, $e_{ia}^A(\omega)$ gauge dependent basis vectors that appear naturally in gauge-covariant derivatives

$$R_{ij}(\theta_g) = \xi_{ij} + e_{ij}^S(-\theta_g) \quad \hat{z} \text{ preserving rotations}$$

$$R_{ab}(\theta_g) = \xi_{ab} + e_{ab}^S(-\theta_g) \quad \hat{z} \text{ preserving gauge transf.}$$

$$e_{ia}^S(\omega) = e_{ia}^S(-\omega) \quad e_{ia}^A(\omega) = -e_{ia}^A(-\omega)$$

Project gauge-covariant field strengths
onto this gauge-rotating basis

$$E_i^a(r, z, t) \Big|_{r < R_0} = E_L(z, t) \xi_{ia} + E_S(z, t) e_{ia}^S(\omega) + E_A(z, t) e_{ia}^A(\omega)$$

$$B_i^a(r, z, t) \Big|_{r < R_0} = B_L(z, t) \xi_{ia} + B_S(z, t) e_{ia}^S(\omega) + B_A(z, t) e_{ia}^A(\omega)$$

with

$$E_L = \partial A_0(z, t) / \partial z - \partial A_1(z, t) / \partial t \quad B_L = a_0^2 - 1$$

$$E_A = 0$$

$$B_A = a_0 (\partial \omega(z, t) / \partial z - A_1(z, t))$$

$$E_S = -a_0 (\partial \omega(z, t) / \partial t - A_0(z, t)) \quad B_S = 0$$

topological current

$$\partial^\mu K_\mu = E_i^a B_i^a$$

$$K_0(r, z, t) \Big|_{r < R_0} = K_0(z, t) = (a_0^2 - 1) A_1(z, t) - a_0^2 \partial \omega(z, t) / \partial z$$

$$K_1(r, z, t) \Big|_{r < R_0} = K_1(z, t) = -(a_0^2 - 1) A_0(z, t) + a_0^2 \partial \omega(z, t) / \partial t$$

Non-Abelian Maxwell's Equations

Induced SU_2 charged current $j_\mu^a(z,t)$

$$j_0^a = J_0(z,t) \hat{z}_a$$

$$j_i^a = J_1(z,t) \hat{x}_{ia} + j_s(z,t) e_{ia}^S(\omega) + j_A(z,t) e_{ia}^A(\omega)$$

$$(\partial_\mu G^{\mu\nu})^a = j_\mu^a \quad \text{and} \quad (\partial_\mu {}^*G^{\mu\nu})^a = 0$$

$$-\partial E_L(z,t)/\partial z + 2a_0 E_S(z,t) = J_0(z,t)$$

$$-\partial E_L(z,t)/\partial t + 2a_0 B_A(z,t) = J_1(z,t)$$

$$-\partial E_S(z,t)/\partial t + \partial B_A(z,t)/\partial z = j_s(z,t)$$

$$(B_A^2 - E_S^2) + B_L(B_L + 1) = a_0 j_A(z,t)$$

$$-E_L(z,t) + a_0 \partial E_S(z,t)/\partial z + a_0 \partial B_A(z,t)/\partial t = \partial^\mu K_\mu = E_i^a B_i^a$$

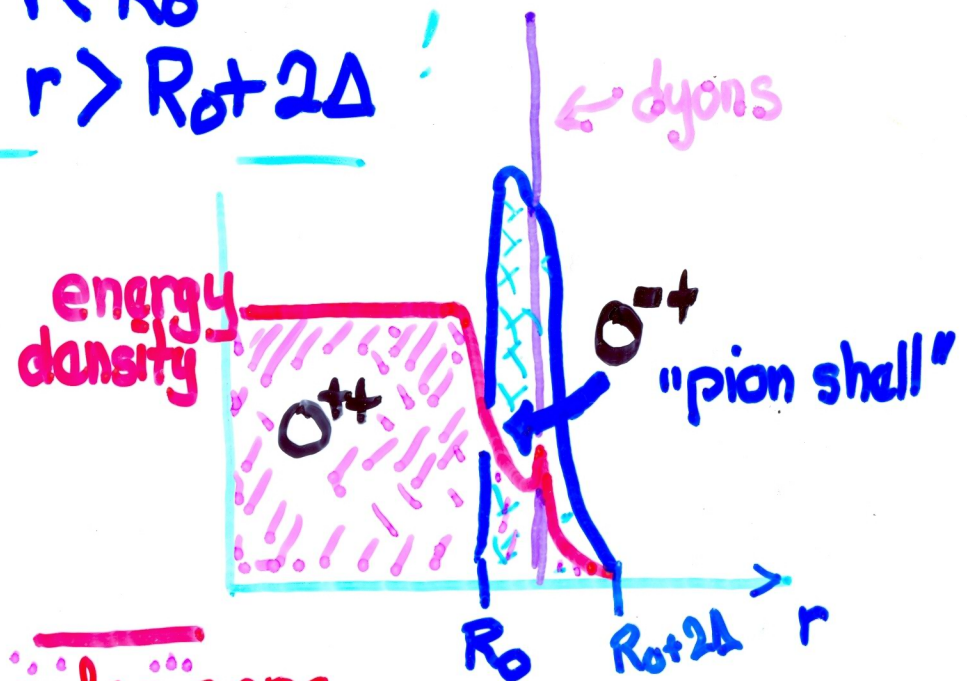
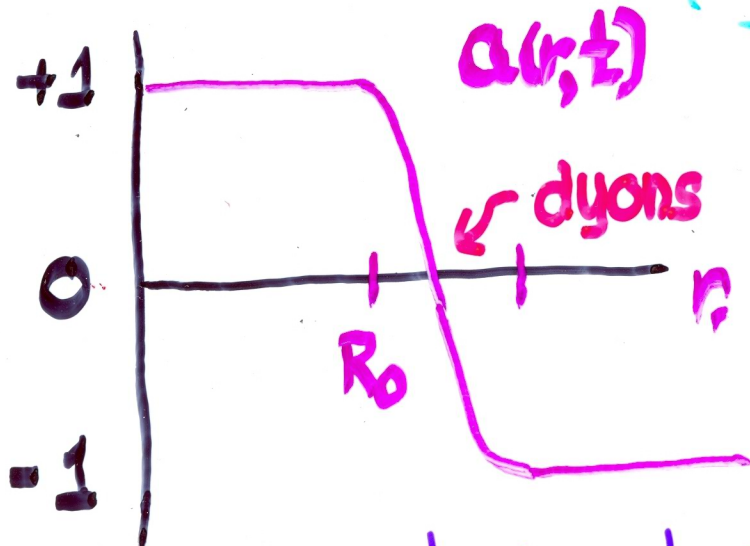
Covariant current conservation $\partial^\mu J_\mu = 2a_0 j_s(z,t)$

FINALLY
 To produce "electric confinement"

$$a_0=1 \Rightarrow B_L(z,t)=0 \Big|_{r < R_0} \quad E_L = E_L^0 + e_L(z,t) \Big|_{r < R_0}$$

$$\begin{aligned} J_0(z,t) &= 2E_S - \partial e_L / \partial z & J_1(z,t) &= 2B_A - \partial e_L / \partial t \\ j_S(z,t) &= \partial B_A / \partial z - \partial E_S / \partial t & j_A(z,t) &= (B_A^2 - E_S^2) \end{aligned} \quad r < R_0$$

$a(r,z,t)$ goes from +1 $r < R_0$
 -1 $r > R_0 + 2\Delta$



QCD Jet: co-axial structure

scalar core

pseudo scalar shell

[Extension to SU(3)]

off-diagonal
gluons carry
charge

$$a=1-3 \text{ SU}(2) \Rightarrow a=1-8 \text{ SU}(3)$$

$$\hat{Z}_a \Rightarrow \hat{Z} |h\rangle_a \quad |h\rangle_a = (h_3, h_8)$$

$$t_3, t_8 \text{ diagonal} \quad t_1-t_2, t_4-t_3 \Rightarrow 3 \text{ SU}(2) \text{ subgroups}$$

$$O(r) \quad G(y) \quad P(b) \quad \text{with } \pm \text{ charge}$$

$$[t_3, Q_O^\pm] = \pm Q_O^\pm \quad [t_3, Q_G^\pm] = \mp \frac{1}{2} Q_G^\pm \quad [t_3, Q_P^\pm] = \mp \frac{1}{2} Q_P^\pm$$

$$[t_8, Q_O] = 0 \quad [t_8, Q_G^\pm] = \mp \frac{\sqrt{3}}{2} Q_G^\pm \quad [t_8, Q_P^\pm] = \pm \frac{\sqrt{3}}{2} Q_P^\pm$$

$$a = (1, 2)$$

$$\xi_{ia} \Rightarrow \xi_{i\bar{a}} \hat{Z}_i \hat{Z} |h\rangle_a$$



$$\sum_c |w_c\rangle = (0, 0)$$

$$a = (4, 5)$$

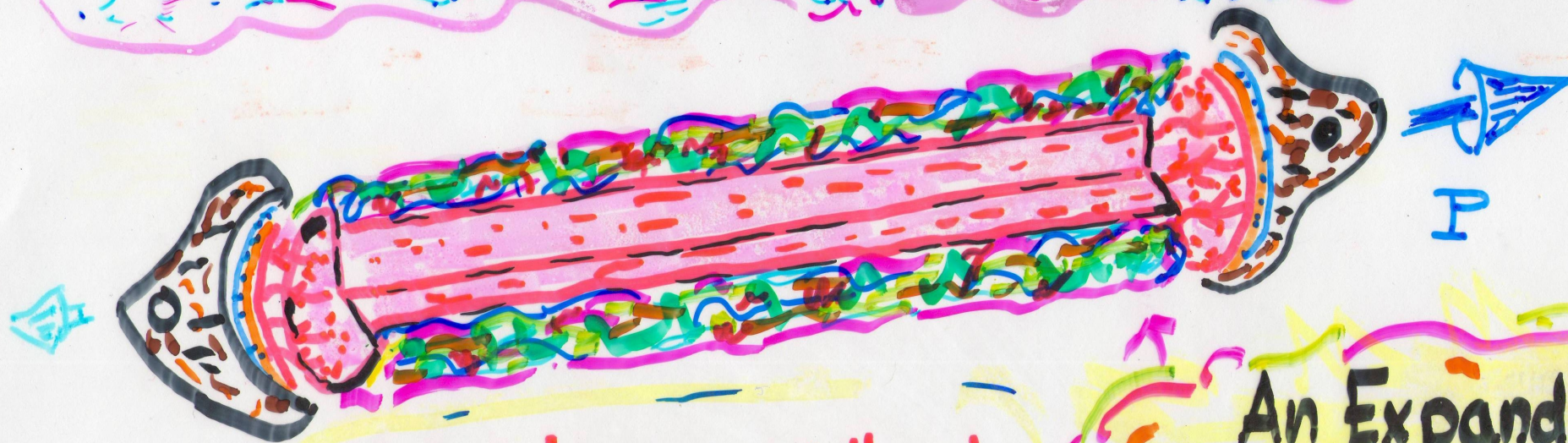
$$e_{ia}^\pm(\omega) \Rightarrow e_{i\bar{a}}^\pm(\sum \omega_a |w_c\rangle)$$

$$|w_0\rangle = (1, 0) \quad |w_4\rangle = (-\frac{1}{2}, -\frac{\sqrt{3}}{2})$$

$$|w_7\rangle = (-\frac{1}{2}, +\frac{\sqrt{3}}{2})$$

"Hawser Laid"

Internal Structure of Jets



Not Sieberg-Witten!

An Expanding
 $SU(3)$ Cylindrical
 Flux Configuration



Radial Sections

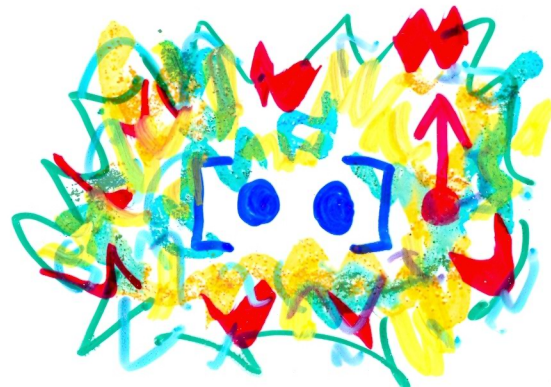
$$r_1 < r_2 < r_3$$

$A_u^a = 0$ vacuum
 + Gribov copies

COLOR TOPOLOGY

the creation of a "new" hadron
involves the RUPTURE of COLOR FLUX

transverse spin observables can
provide important new insight into
this nonperturbative process



$\Delta_\circ \uparrow$ local sign
of $\bullet \uparrow$
polarized s quark

I TRANSVERSE SPIN CONFINEMENT & XSB!

See also: The Adventure
and The Prize
d.sivers arXiv:1109.2521

"Quantum Yang Mills
Theory" Clay Math. Inst.
2000 Jaffe, Witten

- (1) A mass gap, Δ .
- (2.) Confinement
- (3.) Chiral symmetry Breaking

$$\mathcal{L}_q = i(\bar{q}_L \gamma^\mu D_\mu q_L + \bar{q}_R \gamma^\mu D_\mu q_R) - m_q(\bar{q}_L q_R + \bar{q}_R q_L)$$

$$SU(n_f)_L \times SU(n_f)_R \times U(1)_L \times U(1)_R \in \text{PQCD}$$

$$m_u = 1.9 \pm 0.2 \text{ MeV}$$

$$m_d = 4.6 \pm 0.3 \text{ MeV}$$

$$m_s = 88. \pm 5.0 \text{ MeV}$$

SPIN-ORBIT
dynamics
 $\sigma = PA_2$

spin-directed
momentum
 δk_{TN}

$$A_N \frac{d\sigma(qq \uparrow \Rightarrow qq)}{d\sigma(qq \Rightarrow qq)} = \frac{\alpha_s(Q)}{\alpha} m_q f(\theta_{cm})$$

Kane, Pumplin
Repko ('78)
(KPR)

THE CLASSIFICATION of single spin observables

Measurements $A(\vec{\sigma}) = \frac{M(\vec{\sigma}) - M(-\vec{\sigma})}{M(\vec{\sigma}) + M(-\vec{\sigma})}$ are ODD

$(\Theta A \Theta^{-1} = -A)$ under an operator Θ that acts on 3-vectors $\{\vec{R}_\alpha\}$ (3-momenta) and axial 3-vectors $\{\vec{\sigma}_\beta\}$ (spins)
 $\Theta \{\vec{R}_\alpha; \vec{\sigma}_\beta\} \Theta^{-1} = \{\vec{R}_\alpha; -\vec{\sigma}_\beta\}$ compared to Parity operator
 $P \{\vec{R}_\alpha; \vec{\sigma}_\beta\} P^{-1} = \{-\vec{R}_\alpha; \vec{\sigma}_\beta\}$. An operator $A_\pi = P\Theta$ then has the effect $A_\pi \{\vec{R}_\alpha, \vec{\sigma}_\beta\} A_\pi^{-1} = \{-\vec{R}_\alpha; -\vec{\sigma}_\beta\}$. These operators form a group:

$P\Theta = A_\pi$, $\Theta A_\pi = P$, $\Theta = P A_\pi$, $P^2 = \Theta^2 = A_\pi^2 = 1 = P\Theta A_\pi$
All Single-Spin Observables

1. P-odd and A_π -even — (W_\pm, Z_0) exchange
2. A_π -odd and P-even — m_q, m_l + spin-orbit dynamics

(nonperturbative)

Idempotent Projection Operators

$$\Pi_\sigma^\pm \otimes \Pi_P^\pm : \Pi_{A_\pi}^\pm$$

A_T -odd observables $K_{TN} = \vec{K}_T \cdot (\hat{\sigma} \times \hat{P})$

a spin-directed momentum generated by an orbital angular momentum \vec{L} . ($m_q \rightarrow 0$)

A_T^{odd}

KPR factorization (Mulders Tangerman)

dstns. : orbital dst'ns. Boer-Mulders fns. - Process dependence
frag. fns. : polarizing f.f. Collins fns. - Rank dependence

Two other consequences

1. $\Pi_0^- = \Pi_P^- \Pi_{A_T}^+ + \Pi_P^+ \Pi_{A_T}^-$; a new approach to process dependence in hadronic $P=$ -asymmetries

2. K_{TN} -odd asymmetries associated with spins measured in the central regions of jet fragmentation
(Λ_0^+ , $\bar{\Lambda}_0^+$, $\Sigma^+\uparrow$, $\bar{\Sigma}^-\uparrow \dots$) \rightarrow new observables

II. Measuring $\Lambda_0 \uparrow \Rightarrow p \pi^-$ and orienting jet fragmentation

The weak decay $\Lambda_0 \uparrow$ provides a self
analyzing measurement of Λ_0 spin. An ensemble
of events



$$\left. \frac{dn_p}{d\Omega_p} \right|_{\sigma_y = +1/2} = (1 + \alpha \cos \theta_p) \quad \left. \frac{dn_p}{d\Omega_p} \right|_{\sigma_y = -1/2} = (1 - \alpha \cos \theta_p)$$

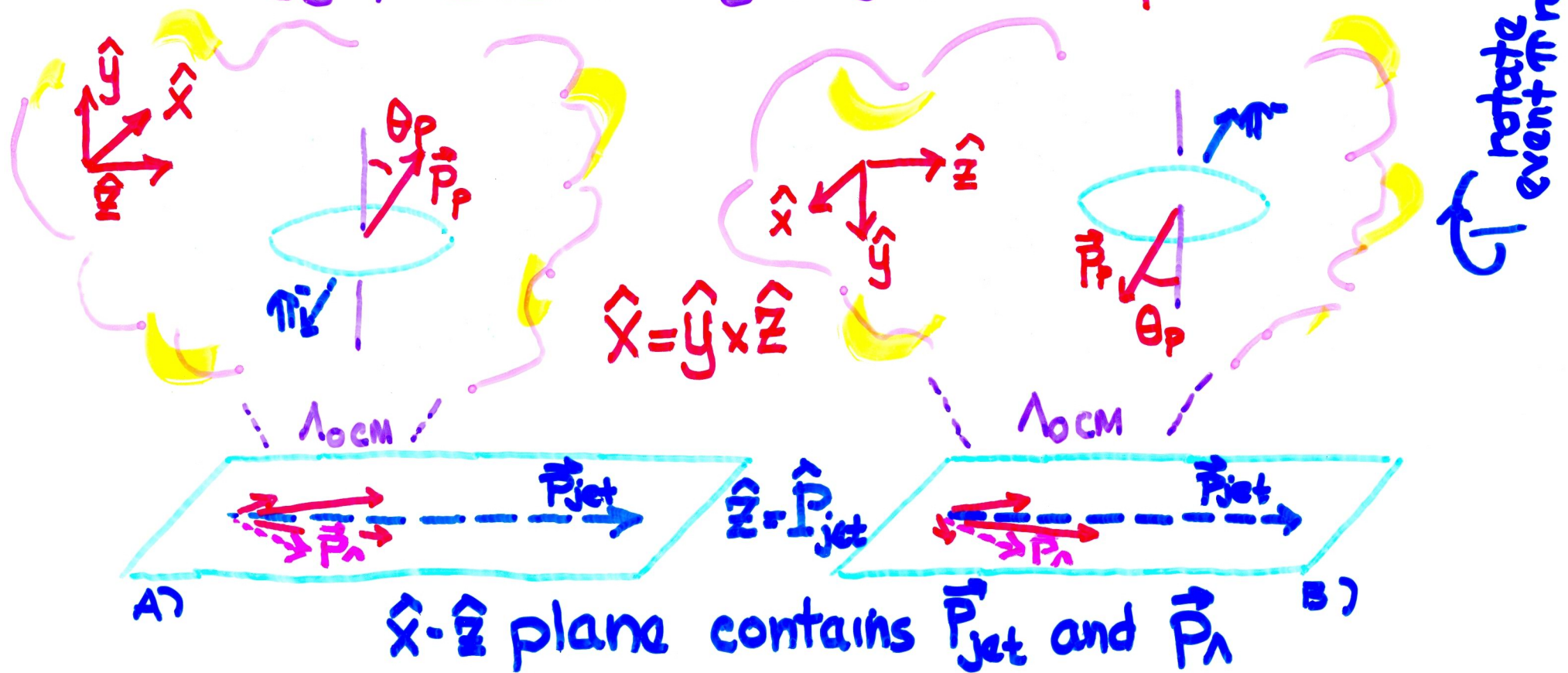
cm system with measured decays

$$P_{\Lambda}^y(\cos \theta_p) = \frac{n_+(\theta_p) - n_-(\theta_p)}{n_+(\theta_p) + n_-(\theta_p)} = \alpha \cos \theta_p$$

with $\alpha \cong 0.642$
analyzing power of
decay

NEW SPIN OBSERVABLES!

Orientation of production plane determined by proton decay angle $\cos\theta_p > 0$



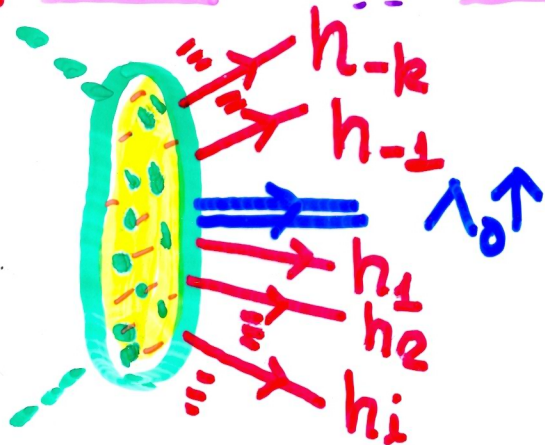
Orientation of spin/directed momentum k_{TN}

$$k_{TN} = \vec{k}_T \cdot (\hat{\sigma}_y \times \hat{P}_{jet}) = \vec{k}_T \cdot \hat{E}_x$$

$$P_\Lambda^y(\cos\theta_p) = \alpha \cos\theta_p > 0$$

ensemble of polarized $\Lambda_0 \uparrow$

Spin-Oriented Particle Density Asymmetries



$$\frac{d^3 \vec{p}_i}{E_i} = d\eta_i dP_T^y dP_T^x = d\eta_i dP_{TS}^i dP_{TN}^i$$

rapidity order particles in jet containing polarized $\Lambda_0 \uparrow$

$$P_\Lambda^\mu = (m_\Lambda^\wedge \cosh \eta_\Lambda, P_{TN}^\wedge \hat{e}_x, m_\Lambda^\wedge \sinh \eta_\Lambda)$$

$$m_\Lambda^\wedge = (m_\Lambda^2 + P_{TN}^2)^{1/2}$$

$$P_i^\mu = (m_T^i \cosh \eta_i, P_{TN}^i \hat{e}_x + P_{TS}^i \hat{e}_y, m_T^i \sinh \eta_i)$$

$$m_T^i = (m_i^2 + P_{TN}^{i2} + P_{TS}^{i2})^{1/2}$$

$$S_{\Lambda i} = m_\Lambda^2 + m_i^2 + 2m_\Lambda^\wedge m_T^i \cosh(\eta_i - \eta_\Lambda) - 2P_{TN}^\wedge P_{TN}^i$$

$$t_{\Lambda i} = m_\Lambda^2 + m_i^2 - 2m_\Lambda^\wedge m_T^i \cosh(\eta_i - \eta_\Lambda) + 2P_{TN}^\wedge P_{TN}^i$$

Λ h systems
Mandelstam
invariants

$$\delta \eta_i = \eta_i - \eta_\Lambda \text{ rapidity diff.}$$

$$\delta P_{TN}^i = P_{TN}^i - P_{TN}^\wedge$$

spin ordered momentum diff

rapidity densities for identified particles (π^- , π^+ , K_S^0 ...etc)
in the neighborhood of Λ_0

$$\pi^-(\delta\eta, \delta P_{TN}) = \sum_{i=\pi^-} \int dP_{TS}^i \frac{d\sigma_{hi}(\delta\eta_i, \delta P_{TN}^i, P_{TS}^i)}{d\eta_i dP_{TN}^i dP_{TS}^i}$$

$$\pi^+(\delta\eta, \delta P_{TN}) = \sum_{i=\pi^+} \int dP_{TS}^i \frac{d\sigma_{hi}(\delta\eta_i, \delta P_{TN}^i, P_{TS}^i)}{d\eta_i dP_{TN}^i dP_{TS}^i}$$

$$K_S^0(\delta\eta, \delta P_{TN}) = \sum_{i=K_S^0} \int dP_{TS}^i \frac{d\sigma_{hi}(\delta\eta_i, \delta P_{TN}^i, P_{TS}^i)}{d\eta_i dP_{TN}^i dP_{TS}^i}$$

can be measured by summing over a large number of
events containing polarized Λ_0 's

Spin-ordered Asymmetries

$$\Delta^N \pi^-(\delta\eta, \delta P_{TN}) = \langle P_N(\cos\theta_P) [\pi^-(\delta\eta, \delta P_{TN}) - \pi^-(\delta\eta, -\delta P_{TN})] \rangle$$

provide unique evidence for non-perturbative,
spin-ordered, mechanisms in the hadronization
phase of the fragmentation process

$\Lambda_0 \uparrow$ provides a valuable local marker for spin orientation and s-quark in fragmentation

$$\Lambda_0 \uparrow \approx [u, d] \times s \uparrow$$

$[u, d] = I = J = 0$ diquark



Spin orbit dynamics in the production of the \bar{s} quark captured by neighboring hadrons

$$\delta\eta_h > 0 \text{ implies } \delta P_{TN}^h < 0$$

$$\delta\eta_h < 0 \text{ implies } \delta P_{TN}^h > 0$$

quantum number density asymmetries

Summing over hadrons
weighted by quantum
numbers

$$\Delta^N S(\delta\eta, 0.1)$$

$\delta\eta$

strangeness
 S

$$\Delta^N Q(\delta\eta, 0.1)$$

$\delta\eta$

charge Q

Spin-dependent

QUANTUM

NUMBER DENSITY

ASYMMETRIES

$$\Delta^N B(\delta\eta, 0.1)$$

$\delta\eta$

B baryon number

IV. Spin-directed density asymmetries

(a localized (in rapidity) tool for studying MEDIUM MODIFICATION of fragmentation dynamics.

NOT AN EXPERT IN HEAVY ION COLLISIONS

H. Pei - "Probing Hot and Dense..." arXiv:1110.1442

H. Caines - "Jets and Jet-like Correlations..." arXiv:1110.1878

T. Renk - "Jets in Medium" arXiv:1111.0769

The comparison of jets pp, pA, AA collisions

Medium Cold nuclear matter
Colored glass condensate
Quark gluon plasma

Inferences based on observables (R_{AA} , I_{AA} ...)

Rupturing a Hawser



in vacuum O^{++} required



Collins functions

$^3P_0 (q\bar{q}) \quad O^{++}$

jet origin in COLD NUCLEAR MATTER



QIM RUPTURE



Bulk

increased multiplicity
jet broadening from
gluon radiation

Local

fewer 3P_0 pairs $\eta < \eta_c$
 $\Lambda \uparrow$ produced near η_c pos.
correlation lengths grow
(esp. for B)

jet
origin
in

QUARK
GLUON PLASMA

Boxcar



Mid-rapidity section of
jet merges with spectators

Bulk

path dependent energy loss
jet broadening

Local

antibaryons absent $\eta < \eta_c$
no 3P_0 pairs $\eta < \eta_c$

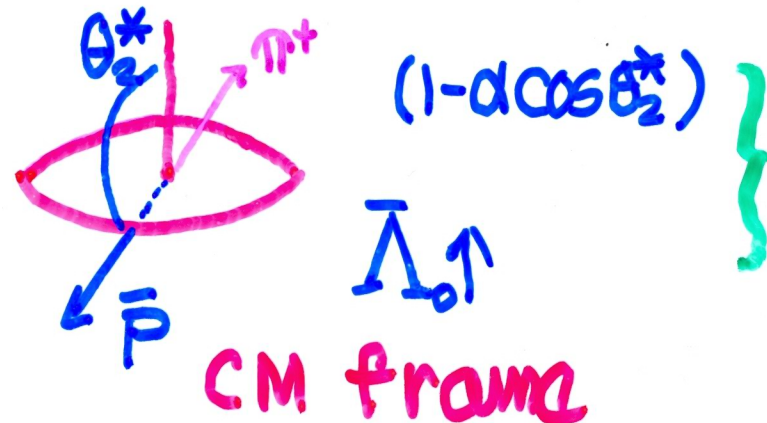
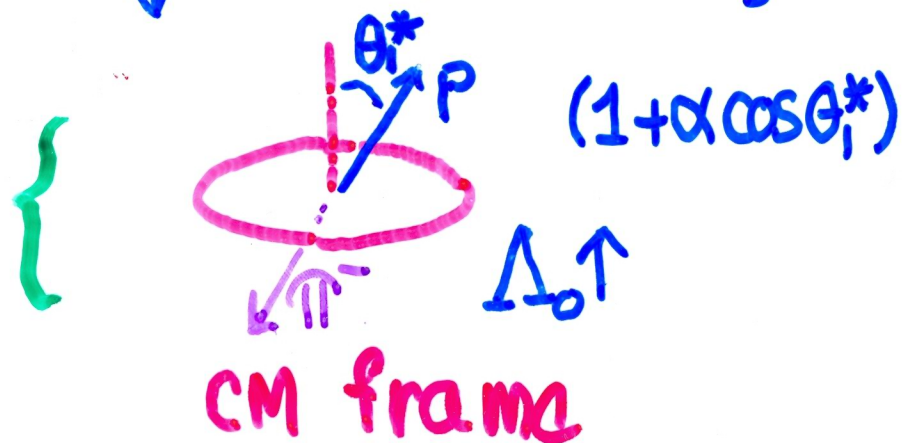
V. Detector Requirements and other spin-directed measurements

Ellis Hwang

SPIN-SPIN CORRELATIONS of $\Lambda_0 \uparrow \Lambda_0 \uparrow$ PAIRS

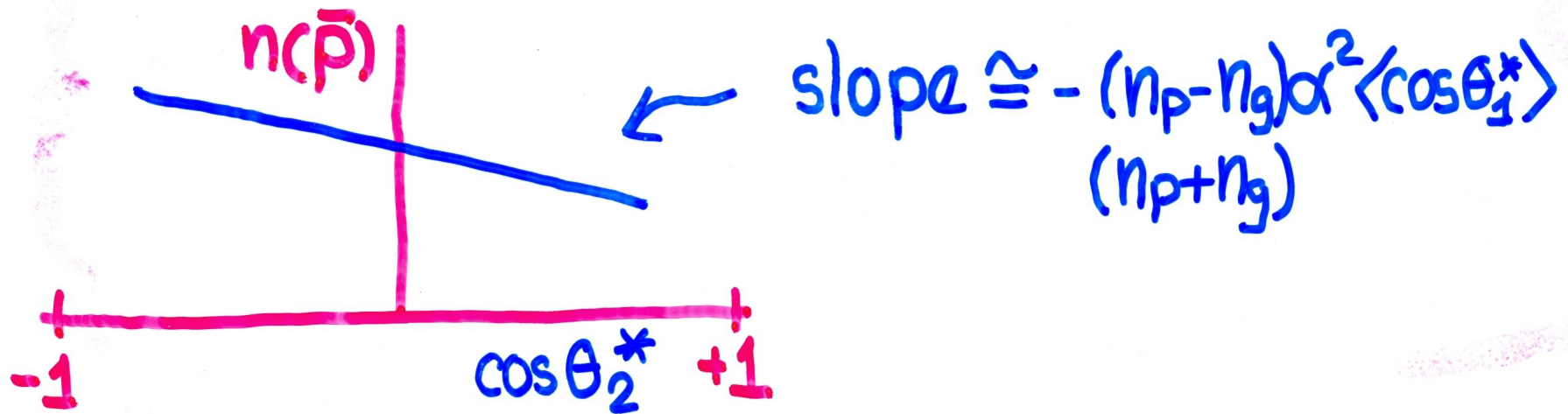
$$\alpha^2 = 0.412$$

$$\left(\begin{array}{l} \uparrow \downarrow \rightarrow \uparrow \downarrow \quad {}^3P_0 \text{ pairs} \Rightarrow \sum_s |M|^2 \alpha \quad n_p (1 - \alpha^2 \cos \theta_1^* \cos \theta_2^*) \\ \uparrow \uparrow \rightarrow \uparrow \uparrow \quad {}^1S_0 \text{ pairs} \Rightarrow \sum_s |M|^2 \alpha \quad n_g (1 + \alpha^2 \cos \theta_1^* \cos \theta_2^*) \end{array} \right)$$



another reason for detecting

$\Delta_0 \uparrow$ (and $\bar{\Delta}_0 \uparrow$) decays



a marker for $\bar{s}s$ production mechanisms
local in rapidity space

DIRECTLY

aids in the normalization of quantum number
density asymmetries !!

EXPERIMENTAL CHALLENGE

1. measure jet axis $\hat{z} = \hat{P}_{\text{jet}}$
2. reconstruct $\Lambda_c \uparrow \Rightarrow p\pi^-$ & measure \vec{p}_Λ
3. determine CM $\theta_p \Rightarrow P_\Lambda^y(\cos\theta_p) = 0.642 \cos\theta_p \geq 0$
4. particle id & momenta \vec{p}_i ($\eta_\Lambda \approx \eta_i$)

Goldstein & Liutti

connect to $\Lambda_c \uparrow, \Lambda_b \uparrow$

Homer Neal
Dan Scheirich

Atlas